

1. Find all the topologies on the set  $X = \{0, 1\}$ . Which ones are Hausdorff?
2. Verify that the co-finite topology is in fact a topology. When is it metrizable?
3. Show that if  $X$  is finite and  $\mathcal{T}$  is a metrizable topology on  $X$  then  $\mathcal{T}$  is the discrete topology.