

1. Let $L : U \rightarrow U$ be a linear transformation. The *spectrum* $\mathcal{S}(L)$ of L is the set of eigenvalues of L . Show that $\mathcal{S}(L + \mu I) = \mathcal{S}(L) + \{\mu\}$ for all $\mu \in \mathbf{F}$.

2. Let $L : U \rightarrow U$ be a linear transformation. Recall that a subspace W of U is L -invariant if $L(W) \subseteq W$. Let μ be a scalar. Show that a subspace W of U is $(L + \mu I)$ -invariant if and only if W is L -invariant.