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In[1]:= (* We compute the surface area of the upper
        hemisphere with radius R centered at the origin *)
r = {R Sin[ph] Cos[th], R Sin[ph] Sin[th], R Cos[ph]};
rt = D[r, th];
rp = D[r, ph];
n = Simplify[Cross[rt, rp]]
nn = Simplify[Norm[n], Assumptions -> R > 0 && 0 < th < 2 Pi && 0 < ph < Pi/2]
Integrate[Integrate[nn, {th, 0, 2 Pi}], {ph, 0, Pi/2}]

Out[4]= {-R^2 Cos[th] Sin[ph]^2, -R^2 Sin[ph]^2 Sin[th], -R^2 Cos[ph] Sin[ph]}

Out[5]= R^2 Sin[ph]

Out[6]= 2 Pi R^2

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