$$f(f^{-1}(x)) = x - \frac{w}{z}$$

$$f^{-1}(x) - \frac{d}{dx}f^{-1}(x) = \frac{w}{z} = \frac{1}{z/w} = \frac{1}{f'(f^{-1}(x))}$$